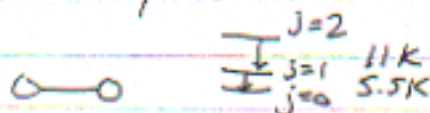


Molecular Clouds H_2

most impt tracer = CO

- high abundance $\sim 5 \times 10^{-5}$ CO/ H_2 molecules
- (next highest abund = dust)
- favorable excitation ~ 5.5 K ($J=1 \rightarrow 0$)
- chemically robust

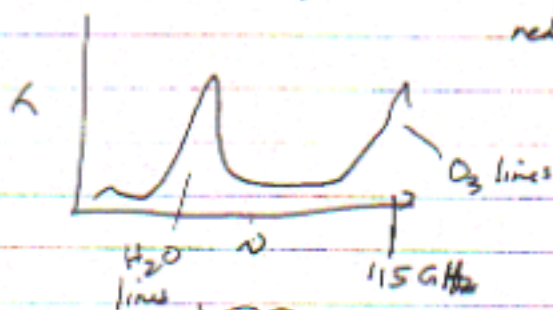


$$h\nu = hB 2(j+1)$$

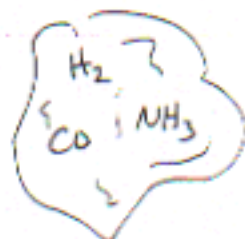
$$\text{rotational constant} = \frac{h}{8\pi^2 I} \quad (\text{units of freq.})$$

$$\nu_{1-0} = 115.27 \text{ GHz}$$

$MR^2 \sim 10^0$
red. mass of C+O \Rightarrow radio freq.



obs. window in Earth atmosphere

Use CO to measure N, T 

cloud

radio telescope

$$\Delta I^{12} = (B(T_{ex}^{12}) - B(T_{bg})) (1 - e^{-\tau_{12}}) \quad (^{12}\text{CO})$$

$$\frac{n_2}{n_1} = \frac{g_1}{g_2} e^{-h\nu/kT_{ex}} \quad \text{LTE} \Rightarrow T_{ex} = T$$

$$B = \frac{2kT\nu^2}{c^2}$$

$$\Delta I^{13} = (B(T_{ex}^{13}) - B(T_{bg})) (1 - e^{-\tau_{13}}) \quad (^{13}\text{CO})$$

if $\tau_{12}, \tau_{13} \ll 1$ and $T_{ex}^{12} = T_{ex}^{13}$

$$\Rightarrow \frac{\Delta I^{12}}{\Delta I^{13}} = \frac{\tau^{12}}{\tau^{13}} = \frac{N^{12}}{N^{13}} = 89 \Rightarrow \text{solar neighborhood, Sun}$$

measure w/ telescope:

"Solar abundance"

$$\frac{\Delta I^{12}}{\Delta I^{13}} \sim 3-5$$

~~approx 3-5~~ ^{12}CO optically thick
 $\Rightarrow \tau_{12} \gg 1$

$$\Rightarrow \frac{\Delta I^{12}}{\Delta I^{13}} \approx \frac{1}{\tau_{13}} \quad ^{13}\text{CO opt. thin.}$$

$$\Delta I^{12} = [B(T_{ex}) - B(T_{bg})] (l) \quad \text{for } \tau_{12} \gg 1$$

$$\tau_0 = \frac{(h\nu)^2}{4\pi k} B_{lu} \phi_{\nu} \frac{N_L}{T_{ex}} \quad (\text{HI})$$

\hookrightarrow line profile

apply to ^{13}CO

$$N_{\text{tot}}(^{13}\text{CO}) = (\text{const}) \tau T_{ex}$$

↑
physics
 ^{13}CO
spectrum

← ^{12}CO

$$N_{\text{tot}}(\text{H}_2) = X N_{\text{tot}}(^{13}\text{CO})$$

(digression)

^{12}CO opt thick, yet measured ^{12}CO still related to $\text{size of cloud}^{\text{mass}}$
 \Rightarrow filling factor, clumpiness